

AMENDMENTS TO CLAIMS

Claim 1 (currently amended): A digital signature cryptographic method comprising:
supplying a set S1 of k polynomial functions as a public-key, the set S1 including the functions $P_1(x_1, \dots, x_{n+v}, y_1, \dots, y_k), \dots, P_k(x_1, \dots, x_{n+v}, y_1, \dots, y_k)$, where k, v, and n are integers, x_1, \dots, x_{n+v} are $n+v$ variables of a first type, y_1, \dots, y_k are k variables of a second type, and the set S1 is obtained by applying a secret key operation on a set S2 of k polynomial functions $P'_1(a_1, \dots, a_{n+v}, y_1, \dots, y_k), \dots, P'_k(a_1, \dots, a_{n+v}, y_1, \dots, y_k)$ where a_1, \dots, a_{n+v} are $n+v$ variables which include a set of n "oil" variables a_1, \dots, a_n , and a set of v "vinegar" variables a_{n+1}, \dots, a_{n+v} , the supplying comprising selecting the number v of "vinegar" variables to be greater than the number n of "oil" variables;

providing a message to be signed;

applying a hash function on the message to produce a series of k values b_1, \dots, b_k ;

substituting the series of k values b_1, \dots, b_k for the variables y_1, \dots, y_k of the set S2 respectively to produce a set S3 of k polynomial functions $P''_1(a_1, \dots, a_{n+v}), \dots, P''_k(a_1, \dots, a_{n+v})$;

selecting v values $a'_{n+1}, \dots, a'_{n+v}$ for the v "vinegar" variables a_{n+1}, \dots, a_{n+v} ;

solving a set of equations $P''_1(a_1, \dots, a_n, a'_{n+1}, \dots, a'_{n+v})=0, \dots, P''_k(a_1, \dots, a_n, a'_{n+1}, \dots, a'_{n+v})=0$ to obtain a solution for a'_1, \dots, a'_n ; and

applying the secret key operation to transform a'_1, \dots, a'_{n+v} to a digital signature e_1, \dots, e_{n+v} .

Claim 2 (previously presented): A method according to claim 1 and also comprising verifying the digital signature.

Claim 3 (previously presented): A method according to claim 2 and wherein said verifying comprises:

obtaining the signature e_1, \dots, e_{n+v} , the message, the hash function and the public key;

applying the hash function on the message to produce the series of k values b_1, \dots, b_k ; and

verifying that the equations $P_1(e_1, \dots, e_{n+v}, b_1, \dots, b_k) = 0, \dots, P_k(e_1, \dots, e_{n+v}, b_1, \dots, b_k) = 0$ are satisfied.

Claim 4 (previously presented): A method according to claim 1 and wherein the method comprises an HFEV scheme and the set S2 comprises a set f(a) of k polynomial functions of the HFEV scheme.

Claim 5 (previously presented): A method according to claim 1 and wherein the method comprises a UOV scheme and the set S2 comprises a set S of k polynomial functions of the UOV scheme.

Claim 6 (canceled)

Claim 7 (previously presented): A method according to claim 1 and wherein v is selected such that q^v is greater than 2^{32} , where q is the number of elements of a finite field K over which the sets S1, S2 and S3 are provided.

Claim 8 (previously presented): A method according to claim 1 and wherein said supplying comprises obtaining the set S1 from a subset S2' of k polynomial functions of the set S2, the subset S2' being characterized in that all coefficients of components involving any of the y_1, \dots, y_k variables in the k polynomial functions $P'_1(a_1, \dots, a_{n+v}, y_1, \dots, y_k), \dots, P'_k(a_1, \dots, a_{n+v}, y_1, \dots, y_k)$ are zero, and the number v of "vinegar" variables is greater than the number n of "oil" variables.

Claim 9 (previously presented): A method according to claim 8 and wherein the set S2 comprises a set S of k polynomial functions of a UOV scheme, and the number v of "vinegar" variables is selected to satisfy one of the following conditions:

- (a) for each characteristic p other than 2 of a field K in an "Oil and Vinegar" scheme of degree 2, v satisfies the inequality $q^{(v-n)-1} * n^4 > 2^{40}$, where K is a finite field over which the sets $S1$, $S2$ and $S3$ are provided,
- (b) for $p = 2$ in an "Oil and Vinegar" scheme of degree 3, v is greater than $n*(1 + \sqrt{3})$ and less than or equal to $n^3/6$, and
- (c) for each p other than 2 in an "Oil and Vinegar" scheme of degree 3, v is greater than n and less than or equal to n^4 .

Claim 10 (previously presented): A method according to claim 8 and wherein the set $S2$ comprises a set S of k polynomial functions of a UOV scheme, and the number v of "vinegar" variables is selected to satisfy the inequalities $v < n^2$ and $q^{(v-n)-1} * n^4 > 2^{40}$ for a characteristic $p=2$ of a field K in an "Oil and Vinegar" scheme of degree 2, where K is a finite field over which the sets $S1$, $S2$ and $S3$ are provided and q is the number of elements of K .

Claim 11 (original): A method according to claim 1 and wherein said secret key operation comprises a secret affine transformation s on the $n+v$ variables a_1, \dots, a_{n+v} .

Claim 12 (original): A method according to claim 4 and wherein said set $S2$ comprises an expression including k functions that are derived from a univariate polynomial.

Claim 13 (original): A method according to claim 12 and wherein said univariate polynomial includes a univariate polynomial of degree less than or equal to 100,000.

Claim 14 (original): A cryptographic method for verifying the digital signature of claim 1, the method comprising:

obtaining the signature e_1, \dots, e_{n+v} , the message, the hash function and the public key;

applying the hash function on the message to produce the series of k values b_1, \dots, b_k ; and

verifying that the equations $P_1(e_1, \dots, e_{n+v}, b_1, \dots, b_k) = 0, \dots, P_k(e_1, \dots, e_{n+v}, b_1, \dots, b_k) = 0$ are satisfied.

Claim 15 (previously presented): In an “Oil and Vinegar” signature method, an improvement comprising using more “vinegar” variables than “oil” variables.

Claim 16 (previously presented): A method according to claim 15 and wherein a number v of “vinegar” variables is selected to satisfy one of the following conditions:

- (a) for each characteristic p other than 2 of a field K and for a degree 2 of the “Oil and Vinegar” signature method, v satisfies the inequality $q^{(v-n)-1} * n^4 > 2^{40}$, where n is a number of “oil” variables, K is a finite field from which the n “oil” variables and the v “vinegar” variables are selected, and q is the number of elements of K,
- (b) for $p = 2$ and for a degree 3 of the “Oil and Vinegar” signature method, v is greater than $n*(1 + \sqrt{3})$ and less than or equal to $n^3/6$, and
- (c) for each p other than 2 and for a degree 3 of the “Oil and Vinegar” signature method, v is greater than n and less than or equal to n^4 .

Claim 17 (previously presented): A method according to claim 15 and wherein a number v of “vinegar” variables is selected to satisfy the inequalities $v < n^2$ and $q^{(v-n)-1} * n^4 > 2^{40}$ for a characteristic $p=2$ of a field K in an “Oil and Vinegar” scheme of degree 2, where n is a number of “oil” variables, K is a finite field from which the n “oil” variables and the v “vinegar” variables are selected, and q is the number of elements of K.

Claim 18 (currently amended): A signature generator comprising:

a signature input receiver operative to receive a set S1 of k polynomial functions as a public-key and a message to be signed, the set S1 including the functions $P_1(x_1, \dots, x_{n+v}, y_1, \dots, y_k), \dots, P_k(x_1, \dots, x_{n+v}, y_1, \dots, y_k)$, where k, v, and n are integers, x_1, \dots, x_{n+v} are $n+v$ variables of a first type, y_1, \dots, y_k are k variables of a second type, and the set S1 is obtained by applying a secret key operation on a set S2 of k polynomial functions $P'_1(a_1, \dots, a_{n+v}, y_1, \dots, y_k), \dots, P'_k(a_1, \dots, a_{n+v}, y_1, \dots, y_k)$, where a_1, \dots, a_{n+v} are $n+v$ variables which include a set of n "oil" variables a_1, \dots, a_n , and a set of v "vinegar" variables a_{n+1}, \dots, a_{n+v} , and the number v of "vinegar" variables is greater than the number n of "oil" variables; and

a signature processor operatively associated with the signature input receiver and operative to perform the following operations:

to apply a hash function on the message to produce a series of k values b_1, \dots, b_k ,

C 1
to substitute the series of k values b_1, \dots, b_k for the variables y_1, \dots, y_k of the set S2 respectively to produce a set S3 of k polynomial functions $P''_1(a_1, \dots, a_{n+v}), \dots, P''_k(a_1, \dots, a_{n+v})$,

to select v values $a'_{n+1}, \dots, a'_{n+v}$ for the v "vinegar" variables a_{n+1}, \dots, a_{n+v} ;

to solve a set of equations $P''_1(a_1, \dots, a_n, a'_{n+1}, \dots, a'_{n+v})=0, \dots, P''_k(a_1, \dots, a_n, a'_{n+1}, \dots, a'_{n+v})=0$ to obtain a solution for a'_1, \dots, a'_n ; and

to apply the secret key operation to transform a'_1, \dots, a'_{n+v} into a digital signature e_1, \dots, e_{n+v} .

Claim 19 (previously presented): Apparatus according to claim 18 and also comprising a signature verifier operatively associated with the signature processor and operative to verify the digital signature.

Claim 20 (previously presented): Apparatus according to claim 19 and wherein said signature verifier is operative to verify the digital signature by performing the following operations:

obtaining the signature e_1, \dots, e_{n+v} , the message, the hash function and the public key;

applying the hash function on the message to produce the series of k values b_1, \dots, b_k ; and

verifying that the equations $P_1(e_1, \dots, e_{n+v}, b_1, \dots, b_k) = 0, \dots, P_k(e_1, \dots, e_{n+v}, b_1, \dots, b_k) = 0$ are satisfied.

Claim 21 (previously presented): Apparatus according to claim 18 and wherein the signature processor is operative to perform an HFEV scheme, and the set S2 comprises a set f(a) of k polynomial functions of the HFEV scheme.

Claim 22 (previously presented): Apparatus according to claim 18 and wherein the signature processor is operative to perform a UOV scheme, and the set S2 comprises a set S of k polynomial functions of the UOV scheme.

C | Claim 23 (canceled)

Claim 24 (previously presented): Apparatus according to claim 18 and wherein v is selected such that q^v is greater than 2^{32} , where q is the number of elements of a finite field K over which the sets S1, S2 and S3 are provided.

Claim 25 (previously presented): Apparatus according to claim 18 and wherein the set S1 is obtained from a subset S2' of k polynomial functions of the set S2, the subset S2' being characterized in that all coefficients of components involving any of the y_1, \dots, y_k variables in the k polynomial functions $P'_1(a_1, \dots, a_{n+v}, y_1, \dots, y_k), \dots, P'_k(a_1, \dots, a_{n+v}, y_1, \dots, y_k)$ are zero, and the number v of "vinegar" variables is greater than the number n of "oil" variables.

Claim 26 (previously presented): Apparatus according to claim 25 and wherein the set S2 comprises a set S of k polynomial functions of a UOV scheme, and the

number v of "vinegar" variables is selected to satisfy one of the following conditions:

- (a) for each characteristic p other than 2 of a field K in an "Oil and Vinegar" scheme of degree 2, v satisfies the inequality $q^{(v-n)-1} * n^4 > 2^{40}$, where K is a finite field over which the sets S1, S2 and S3 are provided,
- (b) for $p = 2$ in an "Oil and Vinegar" scheme of degree 3, v is greater than $n*(1 + \sqrt{3})$ and less than or equal to $n^3/6$, and
- (c) for each p other than 2 in an "Oil and Vinegar" scheme of degree 3, v is greater than n and less than or equal to n^4 .

Claim 27 (currently amended): Apparatus according to claim 25 and wherein the set S2 comprises a set S of k polynomial functions of a UOV scheme, and the number v of "vinegar" variables is selected to satisfy the inequalities $v < n^2$ and $q^{(v-n)-1} * n^4 > 2^{40}$ for a characteristic $p=2$ of a field K in an "Oil and Vinegar" scheme of degree 2, [[2,]], where K is a finite field over which the sets S1, S2 and S3 are provided and q is the number of elements of K.

Claim 28 (previously presented): Apparatus according to claim 18 and wherein said secret key operation comprises a secret affine transformation s on the $n+v$ variables a_1, \dots, a_{n+v} .

Claim 29 (previously presented): Apparatus according to claim 21 and wherein said set S2 comprises an expression including k functions that are derived from a univariate polynomial.

Claim 30 (previously presented): Apparatus according to claim 29 and wherein said univariate polynomial includes a univariate polynomial of degree less than or equal to 100,000.

Claim 31 (previously presented): A signature verifier for verifying the digital signature generated by the signature generator of claim 18, the signature verifier comprising a verifier processor operative to perform the following operations:

to obtain the signature e_1, \dots, e_{n+v} , the message, the hash function and the public key via the signature input receiver;

to apply the hash function on the message to produce the series of k values b_1, \dots, b_k ; and

to verify that the equations $P_1(e_1, \dots, e_{n+v}, b_1, \dots, b_k) = 0, \dots, P_k(e_1, \dots, e_{n+v}, b_1, \dots, b_k) = 0$ are satisfied.

Claim 32 (previously presented): In an “Oil and Vinegar” signature generating apparatus an improvement characterized in that the “Oil and Vinegar” signature generating apparatus is operative to use more “vinegar” variables than “oil” variables.

C
Claim 33 (currently amended): An “Oil and Vinegar” signature generating apparatus according to claim 32 and wherein a number v of “vinegar” variables is selected to satisfy one of the following conditions:

(a) for each characteristic p other than 2 of a field K and for a degree 2 of an “Oil and Vinegar” signature method, v satisfies the inequality $q^{(v-n)-1} * n^4 > 2^{40}$, where n is a number of “oil” variables, K is a finite field from which the n “oil” variables and the v “vinegar” variables are selected, and q is the number of elements of K,

(b) for $p = 2$ and for a degree 3 of the “Oil and Vinegar” signature method, v is greater than $n*(1 + \sqrt{3})$ and less than or equal to $n^3/6$, and

(c) for each p other than 2 and for a degree 3 of the “Oil and Vinegar” signature method, v is greater than n and less than or equal to n^4 .

Claim 34 (previously presented): An “Oil and Vinegar” signature generating apparatus according to claim 32 and wherein a number v of “vinegar” variables is

selected to satisfy the inequalities $v < n^2$ and $q^{(v-n)-1} * n^4 > 2^{40}$ for a characteristic $p=2$ of a field K in an "Oil and Vinegar" scheme of degree 2, where n is a number of "oil" variables, K is a finite field from which the n "oil" variables and the v "vinegar" variables are selected, and q is the number of elements of K .

Claim 35 (currently amended): A digital signature comprising:

a signature e_1, \dots, e_{n+v} generated by processing a set $S1$ of k polynomial functions provided as a public-key and a message to be signed, where the set $S1$ includes functions $P_1(x_1, \dots, x_{n+v}, y_1, \dots, y_k), \dots, P_k(x_1, \dots, x_{n+v}, y_1, \dots, y_k), \dots, P_k(x_1, \dots, x_{n+v}, y_1, \dots, y_k)$, where k , v , and n are integers, x_1, \dots, x_{n+v} are $n+v$ variables of a first type, y_1, \dots, y_k are k variables of a second type, and the set $S1$ is obtained by applying a secret key operation on a set $S2$ of k polynomial functions $P'_1(a_1, \dots, a_{n+v}, y_1, \dots, y_k), \dots, P'_k(a_1, \dots, a_{n+v}, y_1, \dots, y_k)$ where a_1, \dots, a_{n+v} are $n+v$ variables which include a set of n "oil" variables a_1, \dots, a_n , and a set of v "vinegar" variables a_{n+1}, \dots, a_{n+v} , and the number v of "vinegar" variables is greater than the number n of "oil" variables, so that a hash function applied on the message to produce a series of k values b_1, \dots, b_k that are substituted for the variables y_1, \dots, y_k of the set $S2$ respectively to produce a set $S3$ of k polynomial functions $P''_1(a_1, \dots, a_{n+v}), \dots, P''_k(a_1, \dots, a_{n+v})$ and v values $a'_{n+1}, \dots, a'_{n+v}$ that are selected for the v "vinegar" variables a_{n+1}, \dots, a_{n+v} , enable to solve a set of equations $P''_1(a_1, \dots, a_n, a'_{n+1}, \dots, a'_{n+v}) = 0, \dots, P''_k(a_1, \dots, a_n, a'_{n+1}, \dots, a'_{n+v}) = 0$ to obtain a solution for a'_1, \dots, a'_n , and application of the secret key operation transforms a'_1, \dots, a'_{n+v} into the digital signature e_1, \dots, e_{n+v} .

Claim 36 (previously presented): A digital signature produced by the method of claim 1.

Claim 37 (previously presented): A method according to claim 1 and wherein said supplying comprises obtaining the set $S1$ from a subset $S2'$ of k polynomial functions of the set $S2$, the subset $S2'$ being characterized in that all coefficients of components involving orders higher than 1 of any of the n "oil" variables a_1, \dots, a_n

and coefficients of components involving multiplication of two or more of the n “oil” variables a_1, \dots, a_n in the k polynomial functions $P'_1(a_1, \dots, a_{n+v}, y_1, \dots, y_k), \dots, P'_k(a_1, \dots, a_{n+v}, y_1, \dots, y_k)$ are zero, and the number v of “vinegar” variables is greater than the number n of “oil” variables.

Claim 38 (previously presented): A method according to claim 37 and wherein the set S2 comprises a set S of k polynomial functions of a UOV scheme, and the number v of “vinegar” variables is selected to satisfy one of the following conditions:

- (a) for each characteristic p other than 2 of a field K in an “Oil and Vinegar” scheme of degree 2, v satisfies the inequality $q^{(v-n)-1} * n^4 > 2^{40}$, where K is a finite field over which the sets S1, S2 and S3 are provided,
- (b) for $p = 2$ in an “Oil and Vinegar” scheme of degree 3, v is greater than $n*(1 + \sqrt{3})$ and less than or equal to $n^3/6$, and
- (c) for each p other than 2 in an “Oil and Vinegar” scheme of degree 3, v is greater than n and less than or equal to n^4 .

Claim 39 (previously presented): A method according to claim 37 and wherein the set S2 comprises a set S of k polynomial functions of a UOV scheme, and the number v of “vinegar” variables is selected to satisfy the inequalities $v < n^2$ and $q^{(v-n)-1} * n^4 > 2^{40}$ for a characteristic $p=2$ of a field K in an “Oil and Vinegar” scheme of degree 2, where K is a finite field over which the sets S1, S2 and S3 are provided and q is the number of elements of K.

Claim 40 (previously presented): Apparatus according to claim 18 and wherein the set S1 is obtained from a subset S2’ of k polynomial functions of the set S2, the subset S2’ being characterized in that all coefficients of components involving orders higher than 1 of any of the n “oil” variables a_1, \dots, a_n and coefficients of components involving multiplication of two or more of the n “oil” variables a_1, \dots, a_n in the k polynomial functions $P'_1(a_1, \dots, a_{n+v}, y_1, \dots, y_k), \dots, P'_k(a_1, \dots, a_{n+v}, y_1, \dots, y_k)$ are

zero, and the number v of "vinegar" variables is greater than the number n of "oil" variables.

Claim 41 (previously presented): Apparatus according to claim 40 and wherein the set S2 comprises a set S of k polynomial functions of a UOV scheme, and the number v of "vinegar" variables is selected to satisfy one of the following conditions:

- (a) for each characteristic p other than 2 of a field K in an "Oil and Vinegar" scheme of degree 2, v satisfies the inequality $q^{(v-n)-1} * n^4 > 2^{40}$, where K is a finite field over which the sets S1, S2 and S3 are provided,
- (b) for $p = 2$ in an "Oil and Vinegar" scheme of degree 3, v is greater than $n*(1 + \sqrt{3})$ and less than or equal to $n^3/6$, and
- (c) for each p other than 2 in an "Oil and Vinegar" scheme of degree 3, v is greater than n and less than or equal to n^4 .

Claim 42 (previously presented): Apparatus according to claim 40 and wherein the set S2 comprises a set S of k polynomial functions of a UOV scheme, and the number v of "vinegar" variables is selected to satisfy the inequalities $v < n^2$ and $q^{(v-n)-1} * n^4 > 2^{40}$ for a characteristic $p=2$ of a field K in an "Oil and Vinegar" scheme of degree 2, where K is a finite field over which the sets S1, S2 and S3 are provided and q is the number of elements of K.